



Faculty of Electrical Engineering and Information Technology Institute of Electromechanical and Electronic Design

# Robust Design and Optimization of Thick Film Accelerometers in COMSOL Multiphysics with OptiY

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European COMSOL Conference 2007





## Outline

- 1. Concept of Tolerance Analysis with OptiY
- 2. Thick Film Accelerometer
- 3. Nominal Optimization
- 4. Tolerance Analysis
- 5. Probabilistic Design
- 6. Conclusions





#### **Virtual Design Process**

- Design parameters must be specified so that all specified requirements are met
- Variability and uncertainty of design parameters (tolerances) caused by:
  - Manufacturing inaccuracy
  - Process uncertainty
  - Scattering of material properties
  - Environmental influences
  - Abrasion
  - Human factors
- This produces variability and uncertainty of performance, functional variables, output parameters, and rejections

### Involving Tolerances into the Design Optimization

- Distributed input parameters
- Deterministic simulation model, e.g.:
  - Analytic model
  - Lumped element model
  - FE-model
  - ...
- Output distributions











### Methods of Computation of Output Distributions (implemented in OptiY)

- Monte-Carlo methods
- Analytic methods:
  - Second Order Analysis (SOA)
  - Reduced SOA (RSOA)

$$f = f_{0} + \sum_{j=1}^{n} \frac{\partial f}{\partial x_{j}} (x_{j} - x_{0}) + \frac{1}{2} \sum_{j=1}^{n} \frac{\partial^{2} f}{\partial x_{j}^{2}} (x_{j} - x_{0})^{2}$$

### Methods of Optimization (implemented in OptiY)

- Grid search
- Hooke-Jeeves method
- Evolutionary algorithms





#### **Steps in Tolerance Analysis and Optimization**

- Nominal Optimization ⇒ Set of design parameters for an optimal function
- System Failure Analysis ⇒ Rejection Probability caused by tolerances
- Sensitivity Analysis ⇒ Importance of the tolerances to the function
- Design for Minimal Rejections
   ⇒ Set of design parameters for an optimal function with regard to the tolerances
- Design for Robustness ⇒ Set of design parameters for minimized scattering of the function

# 2. Thick Film Accelerometer

### Working Principle

- Elements:
  - Seismic mass M
  - Leaf springs S
  - Bonded frame F
  - Piezo-Resistors P
  - Measuring Bridge
- Sensitive for acceleration in zdirection
- Cross sensitive for accelerations in x-, y-direction











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# 2. Thick Film Accelerometer

### Working Model

- Made of Low Temperature Cofired Ceramics (LTCC)
- Manufactured at the Fraunhofer-Institute for Ceramic Technologies and Systems, Dresden, Germany
- Characterization by a vibration exciter







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# 2. Thick Film Accelerometer

### COMSOL Multiphysics Model

- Excitation far from resonance ⇒ static structural mechanics model
- Plane symmetry ⇒ one half sensor is modeled
- Linear material, small deformations
- Acceleration as a volume force
- Lower boundary of the frame is fixed
- 40.000 DOF's







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# 2. Thick Film Accelerometer

### **COMSOL Multiphysics Model**

- Mean normal strain in the piezo-resistors measures ΔR
- Solved for:
  - Sensitivity S to acceleration in z-direction
  - cross sensitivity CS to acceleration in y-direction
  - First resonance frequency  $f_R$



$$\frac{\Delta R}{R} = e_{ym} \cdot k$$

$$S = \frac{U_b}{U_s \cdot a_z} = \frac{\Delta R}{2R \cdot a_z} = \frac{e_{ym} \cdot k}{2a_z}$$

$$CS = \frac{U_b}{U_s \cdot a_y} = \frac{\Delta R}{2R \cdot a_y} = \frac{e_{ym} \cdot k}{2a_y}$$









## 2. Thick Film Accelerometer

### Coupling of OptiY and COMSOL Multiphysics



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## 3. Nominal Optimization

#### Input Parameters for optimization:

- Length  $L_{spr}$  and width  $W_{spr}$  of the leaf springs
- Length  $L_m$  and width  $W_m$  of the seismic mass
- Length L<sub>pr</sub> of the piezo-resistor
- Distance B<sub>pr</sub> between the piezo-resistor and the frame

#### **Output Parameters for Optimization:**

- Sensitivity *S*
- Rel. cross sensitivity  $CS_{rel} = CS / S$
- First resonance frequency  $f_R$

 $\Rightarrow$  find maximum, 50  $\mu V/(V^{\star}g)$  expected

- $\Rightarrow$  constrained [0; 2%]
- $\Rightarrow$  constrained [230 Hz; 260 Hz]







### 3. Nominal Optimization

#### **Optimization Process**



#### Function variables iteration process







# 3. Nominal Optimization

#### **Performance Parameters:**

| Funtional Parameter        | Constraint       | Start Value   | Optimal Value |
|----------------------------|------------------|---------------|---------------|
| Sensitivity                | find maximum     | 27,6 μV/(V*g) | 47,6 μV/(V*g) |
| Relative Cross Sensitivity | [0; 2%]          | 1,76 %        | 1,8 %         |
| 1. Resonance Frequency     | [230 Hz; 260 Hz] | 293,7 Hz      | 230,0 Hz      |





### 4. Tolerance Analysis

### **System Failure Analysis**



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## 5. Probabilistic Design

### Minimizing Rejections (Design for Minimum Rejections)



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### 5. Probabilistic Design



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# 5. Probabilistic Design

#### **Performance Parameters:**



| Funtional Parameter        | Constraint       | Start Value      | Optimal<br>Value | Robust<br>Value  |
|----------------------------|------------------|------------------|------------------|------------------|
| Sensitivity                | find maximum     | 27,6<br>μV/(V*g) | 47,6<br>μV/(V*g) | 46,4<br>μV/(V*g) |
| Relative Cross Sensitivity | [0; 2%]          | 1,76 %           | 1,8 %            | 1,8 %            |
| 1. Resonance Frequency     | [230 Hz; 260 Hz] | 293,7 Hz         | 230,0 Hz         | 234,0 Hz         |





## 6. Conclusions

- OptiY and COMSOL Multiphysics are easy to connect at the script interface
- OptiY tool allows to perform different numerical experiments, e.g.
  - Nominal optimization
  - Tolerance analysis (sensitivity analysis, failure probability)
  - Probability based design optimization (design for minimal rejections, design for robustness)
- Solution times (COMSOL model requires 5 minutes to solve, 3 tolerances):
  - Nominal optimization: 1 day
  - Tolerance analysis: 1 hour
  - Probability based design optimization: 1 week
- Probability based design was performed for an thick film accelerometer